

Ellipse

1. For the ellipse  $x^2 + 4y^2 = 9$   
 (a) The eccentricity is  $\frac{1}{2}$  (b) The latus rectum is  $\frac{2}{3}$  (c) A focus is  $(3\sqrt{3}, 0)$  (d) A directrix is  $x = 2\sqrt{3}$
2. The maximum area of an isosceles triangle inscribed in the ellipse  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$  with the vertex at one end of the major axis is  
 (a)  $\sqrt{3}ab$  (b)  $\frac{3\sqrt{3}}{4}ab$  (c)  $\frac{5\sqrt{3}}{4}ab$  (d) None of these
3. The eccentricity of the curve represented by the equation  $x^2 + 2y^2 - 2x + 3y + 2 = 0$  is  
 (a) 0 (b)  $1/2$  (c)  $1/\sqrt{2}$  (d)  $\sqrt{2}$
4. The line  $x \cos \alpha + y \sin \alpha = p$  will be a tangent to the conic  $\frac{x^2}{a^2} + \frac{y^2}{b^2} = 1$ , if  
 (a)  $p^2 = a^2 \sin^2 \alpha + b^2 \cos^2 \alpha$  (b)  $p^2 = a^2 + b^2$   
 (c)  $p^2 = b^2 \sin^2 \alpha + a^2 \cos^2 \alpha$  (d) None of these
5. The radius of the circle passing through the foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$  and having its centre  $(0, 3)$  is  
 (a) 4 (b) 3 (c)  $\sqrt{12}$  (d)  $\frac{7}{2}$
6. The equation  $\frac{x^2}{1-r} - \frac{y^2}{1+r} = 1$ ,  $r > 1$  represents  
 (a) An ellipse (b) A hyperbola (c) A circle (d) An imaginary ellipse
7. The radius of the circle having its centre at  $(0, 3)$  and passing through the foci of the ellipse  $\frac{x^2}{16} + \frac{y^2}{9} = 1$ , is  
 (a) 3 (b) 3.5 (c) 4 (d)  $\sqrt{12}$
8. The locus of a variable point whose distance from  $(-2, 0)$  is  $\frac{2}{3}$  times its distance from the line  $x = -\frac{9}{2}$ , is  
 (a) Ellipse (b) Parabola (c) Hyperbola (d) None of these
9. If  $A$  and  $B$  are two fixed points and  $P$  is a variable point such that  $PA + PB = 4$ , where  $AB < 4$ , then the locus of  $P$  is  
 (a) A parabola (b) An ellipse (c) A hyperbola (d) None of these
10. Equation of the ellipse whose focus is  $(6, 7)$  directrix is  $x + y + 2 = 0$  and  $e = 1/\sqrt{3}$  is  
 (a)  $5x^2 + 2xy + 5y^2 - 76x - 88y + 506 = 0$  (b)  $5x^2 - 2xy + 5y^2 - 76x - 88y + 506 = 0$   
 (c)  $5x^2 - 2xy + 5y^2 + 76x + 88y - 506 = 0$  (d) None of these
11. The equation of the ellipse whose foci are  $(\pm 5, 0)$  and one of its directrix is  $5x = 36$ , is  
 (a)  $\frac{x^2}{36} + \frac{y^2}{11} = 1$  (b)  $\frac{x^2}{6} + \frac{y^2}{\sqrt{11}} = 1$  (c)  $\frac{x^2}{6} + \frac{y^2}{11} = 1$  (d) None of these
12. The equation of ellipse whose distance between the foci is equal to 8 and distance between the directrix is 18, is  
 (a)  $5x^2 - 9y^2 = 180$  (b)  $9x^2 + 5y^2 = 180$  (c)  $x^2 + 9y^2 = 180$  (d)  $5x^2 + 9y^2 = 180$
13. The equation of the ellipse whose one of the vertices is  $(0, 7)$  and the corresponding directrix is  $y = 12$ , is  
 (a)  $95x^2 + 144y^2 = 4655$  (b)  $144x^2 + 95y^2 = 4655$  (c)  $95x^2 + 144y^2 = 13680$  (d) None of these
14. Equations  $x = a \cos \theta$ ,  $y = b \sin \theta$  ( $a > b$ ) represent a conic section whose eccentricity  $e$  is given by  
 (a)  $e^2 = \frac{a^2 + b^2}{a^2}$  (b)  $e^2 = \frac{a^2 + b^2}{b^2}$  (c)  $e^2 = \frac{a^2 - b^2}{a^2}$  (d)  $e^2 = \frac{a^2 - b^2}{b^2}$
15. The curve with parametric equations  $x = 1 + 4 \cos \theta$ ,  $y = 2 + 3 \sin \theta$  is  
 (a) An ellipse (b) A parabola (c) A hyperbola (d) A circle